

Math 2 UNIT 3 OVERVIEW: Rational & Radical Functions Parent Guide

<p align="center">Unit Outcomes</p> <p align="center">At the end of this unit, your student should be able to:</p>	<p align="center">Key Vocabulary</p> <p align="center">Terms to deepen the student's understanding</p>
<ul style="list-style-type: none"> ✓ Identify the parts of a square root expression ✓ Identify the parts of an inverse variation expression ✓ Interpret a square root expression made up of multiple parts ✓ Create equations and inequalities in one variable that represent square root and inverse variation relationships between quantities and use them to solve problems. ✓ Create and graph in two variables to represent square root and inverse variation relationships between quantities. ✓ Create systems of equations including the square root and inverse variation functions to model situations in context. ✓ Use mathematical reasoning to justify a chosen solution method for square root and inverse variation. ✓ Use mathematical reasoning to justify each step of the solving process for square root and inverse variation. ✓ Identify the point of intersection as the solution to a system of equations. ✓ Approximate solutions using graphing technology or successive approximations with a table of values. ✓ Interpret key features of a square root and inverse variation function in context, including positive/negative slope, increasing/decreasing, intercepts, and domain/range when given the function as a table, graph, and/or verbal description. ✓ Generate different representations of square root function and inverse variation functions to show key features. ✓ Compare key features of two functions each with different representation. ✓ Write a function that describes an inverse relationship between two quantities given a graph, a description or ordered pairs. ✓ Rewrite expressions with radicals as expressions with rational exponents and vice versa. 	<ul style="list-style-type: none"> ✓ Rational expression ✓ radical ✓ radicand ✓ base ✓ index ✓ extraneous roots ✓ parent graph ✓ Asymptote ✓ Direct variation ✓ inverse variation ✓ joint variation ✓ constant of variation ✓ Transformations ✓ Translation ✓ Reflection ✓ Dilation ✓ system

Math 2 UNIT 3 OVERVIEW: Rational & Radical Functions Parent Guide

- ✓ Apply the properties of exponents to expressions with rational exponents.
- ✓ Determine if a solution is an extraneous solution to an inverse variation or square root equation.

Understand...

- Each individual part of the square root expression has an effect on the graph of the function.
- Each individual part of the inverse variation expression has an effect on the graph of the function.
- The context which would require a square root or inverse variation to represent it.
- The relationship between the equation and transformations for square root and inverse variation.
- The solution to a system of equations is the point of intersection of the two functions.
- What the solution of a square root or inverse equation represents in the context of the situation.
- There are multiple ways to solve equations and that I must be able to justify my method using appropriate mathematical reasoning.
- The relationship between the solution to a system of two equations and the graphical representation of that solution.
- The different components of a square root function and an inverse variation function and the effect of constants and coefficients in different parts of the function on domain/range, increase/decrease, max/min, symmetry and end behavior.
- The relationship between the symbolic, graphical, numerical, and verbal description of two functions.
- The context of the situation in which an inverse variation function describes the relationship between two variables.
- The position of a constant within an inverse variation and square root function has an effect on its graphical representation.
- The effects of the graphical and tabular representations of a square root and inverse variation function f with $k \cdot f(x)$, $f(x) + k$, $f(x + k)$ for specific values of k (both positive and negative).
- Expressions with rational exponents can be rewritten as radical expressions.
- How extraneous solutions are produced.

Key Standards Addressed

Where This Unit Fits

Math 2 UNIT 3 OVERVIEW: Rational & Radical Functions Parent Guide

Connections to Common Core/NC Essential Standards	Connections to prior and future learning
<p>NC.M2.N-RN.1 Explain how expressions with rational expressions can be rewritten as radical expressions.</p> <p>NC.M2.N-RN.2 Rewrite expressions with radicals and rational exponents into equivalent expressions using the properties of exponents.</p> <p>NC.M2.A-SSE.1 Interpret expressions that represent a quantity in terms of its context.</p> <ol style="list-style-type: none"> Identify and interpret parts of a quadratic, square root, inverse variation, or right triangle trigonometric expression, including terms, factors, coefficients, radicands, and exponents. Interpret quadratic and square root expressions made of multiple parts as a combination of single entities to give meaning in terms of a context. <p>NC.M2.A-CED.1 Create equations and inequalities in one variable that represent quadratic, square root, inverse variation, and right triangle trigonometric relationships and use them to solve problems.</p> <p>NC.M2.A-CED.2 Create and graph equations in two variables to represent quadratic, square root and inverse variation relationships between quantities.</p> <p>NC.M2.A-CED.3 Create systems of linear, quadratic, square root, and inverse variation equations to model situations in context.</p> <p>NC.M2.A-REI.1 Justify a chosen solution method and each step of the solving process for quadratic, square root and inverse variation equations using mathematical reasoning.</p> <p>NC.M2.A-REI.2 Solve and interpret one variable inverse variation and square root equations arising from a context, and explain how extraneous solutions may be produced.</p> <p>NC.M2.A-REI.11 Extend the understanding that the x-coordinate of the points where the</p>	<p>Coming into this unit, students should have a strong foundation in:</p> <p><i>NOTE: In 8th grade math students will have worked with square roots as well as direct variation. In unit 2 of Math 2 they would have also worked with simplifying square roots while solving quadratics with the quadratic formula.</i></p> <ul style="list-style-type: none"> ✓ Using systems to solve an equation of any type. ✓ Interpret key features of graphs, tables, and verbal descriptions in context to describe linear and quadratic functions that arise in applications relating two quantities, including: domain and range, rate of change, symmetries, and end behavior. ✓ Analyze quadratic functions by generating different representations, by hand in simple cases and using technology for more complicated cases, to show key features, including: domain and range; intercepts; intervals where the function is increasing, decreasing, positive, or negative; rate of change; maximums and minimums; symmetries; and end behavior. <p>This unit builds to the following future skills and concepts:</p> <ul style="list-style-type: none"> ✓ Continue work of rational functions with polynomials in M3 ✓ Continue the work of radicals of other indexes in M3 ✓ Continue the work on inverse functions ✓ Continue to build on graphing all functions with key features (including end behavior, increasing, decreasing, intercepts,

Math 2 UNIT 3 OVERVIEW: Rational & Radical Functions Parent Guide

graphs of two square root and/or inverse variation equations $y = \sqrt{x}$ and $y = \frac{1}{\sqrt{x}}$ intersect are the solutions of the equation $\sqrt{x} = \frac{1}{\sqrt{x}}$ and approximate solutions using graphing technology or successive approximations with a table of values.

NC.M2.F-IF.4 Interpret key features of graphs, tables, and verbal descriptions in context to describe functions that arise in applications relating two quantities, including: domain and range, rate of change, symmetries, and end behavior.

NC.M2.F-IF.7 Analyze quadratic, **square root**, and **inverse variation** functions by generating different representations, by hand in simple cases and using technology for more complicated cases, to show key features, including: domain and range; intercepts; intervals where the function is increasing, decreasing, positive, or negative; rate of change; maximums and minimums; symmetries; and end behavior.

NC.M2.F-IF.9 Compare key features of two functions (linear, quadratic, square root, or inverse variation functions) each with a different representation (symbolically, graphically, numerically in tables, or by verbal descriptions).

NC.M2.F-BF.1 Write a function that describes a relationship between two quantities by building quadratic functions with real solution(s) and **inverse variation** functions given a graph, a description of a relationship, or ordered pairs (include reading these from a table).

NC.M2.F-BF.3 Understand the effects of the graphical and tabular representations of a linear, quadratic, **square root**, and **inverse variation** function f with $k \cdot f(x)$, $f(kx)$, $f(x+k)$ for specific values of k (both positive and negative).

max, min, transformations)

Additional Resources

Materials to support understanding and enrichment

Math 2 UNIT 3 OVERVIEW: Rational & Radical Functions Parent Guide

- [Working with Direct, Joint, Inverse, and Combination Variations](#)
- [Direct Variation](#)
- [Inverse Variation](#)
- [Variation Equations](#)
- [Simplifying Radical Expressions](#)
- [Fractional Exponents](#)
- [Transforming Functions](#)
- [Graphing Radical Functions](#)
- [Graphing Radical Functions \(including domain and range\)](#)
- [Radicals Vocabulary Quiz](#)
- [Solve Rational Equations](#)
- [Finding the Zeros to Radical Functions](#)
- [Solving Equations with Radicals inside Radicals](#)

* **Please note**, the unit guides are a work in progress. If you have feedback or suggestions on improvement, please feel free to contact sdupree@wcpss.net.